

Vectors and Vector Products

Goal: Master the use of these basic vector operations; you will need them easily at your beck & call!

Show all of your work in full detail with complete mathematical statements!

Add/subtract the following vectors:

1. $(3\hat{i} + 2\hat{j}) + (\hat{i} + 5\hat{j})$
2. $(-\hat{i} + \hat{j}) + (6\hat{i} + 4\hat{j})$
3. $(6\hat{i} + 2\hat{j}) + (-7\hat{i} + 3\hat{j})$
4. $(x\hat{i} + 4x\hat{j}) + (3\hat{i} + 2y\hat{j})$
5. $(3x^2\hat{i} + xy^2\hat{j}) + (y^3\hat{i} + 4y\hat{j})$
6. $(2xe^{2x}\hat{i} + 2\sin\theta\hat{j}) + (3\cos\theta\hat{i} + 2y^4\hat{j})$

Find the following scalar products:

7. $(3\hat{i} + 2\hat{j}) \cdot (\hat{i} + 5\hat{j})$
8. $(3x\hat{i} + 2x\hat{j}) \cdot (7x\hat{i} + 5y\hat{j})$
9. $(2\hat{i} - 3\hat{j} + \hat{k}) \cdot (3\hat{i} + 2\hat{j} + 4\hat{k})$
10. $(2x\hat{i} + y\hat{j} + xz^2\hat{k}) \cdot (3\hat{i} + 2z\hat{j} + 3y^2\hat{k})$
11. $(3\hat{j} + 2\hat{k}) \cdot (\hat{i} - 5e^{2x}\hat{j})$
12. $(2x^2\hat{i} - x\hat{j} + \hat{k}) \cdot (3\hat{i} + 2x\hat{j} - 4x^2\hat{k})$

Compute the following vector products (use a separate page AND use determinants!):

13. $(3\hat{i} + 2\hat{j}) \times (\hat{i} + 5\hat{j})$
14. $(\hat{i} + \hat{k}) \times \hat{j}$
15. $(2\hat{i} - 3\hat{k}) \times (-4\hat{i} + 6\hat{k})$
16. $(\hat{i} + 3\hat{j} + \hat{k}) \times (-\hat{i} - 2\hat{j} + \hat{k})$
17. $(x^2\hat{i} + y\hat{j} + z^3\hat{k}) \times (xyz\hat{j})$
18. $(2x\hat{i} - 3x\hat{j}) \times (y\hat{j} + e^{xy}\hat{k})$